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Interference Model and Antenna Parameters Setting Effects on 4G-LTE Networks Coverage

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ABSTRACT
The currently emerging Long Term Evolution 4G-LTE cellular networks are based on new technique of transmission called the Orthogonal Frequency Division Multiple Access (OFDMA). This paper shows the interest of robust approach due to the uncertainty of traffic distribution. First, we develop and validate the interference model based on SINR metric for the deployment of the LTE network, and then we use greedy algorithms to show how frequency and tilt parameter settings can impact the coverage performance metric. Two frequency schemes have been compared to validate our model: the frequency reuse 1 scheme whereby the whole available bandwidth is used in each cell/sector and the frequency reuse 3 scheme in which the entire bandwidth is divided into 3 non-overlapping groups and assigned to 3 co-site sectors within each cell.

Categories and Subject Descriptors
C.2.1 [Computer-Communication networks]: Wireless communication; I.6.5 [Simulation and Modeling]: Model development- modeling methodologies

General Terms

Keywords
LTE; SINR; Interference; frequency optimization; tilt optimization; robustness.

1. INTRODUCTION
Looking at the recent development of mobile radio access networks, it appears that size and complexity of cellular networks is growing at breakneck speed.

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has been widely accepted as a promising air-interface technology for future generation systems by various standardization bodies and forums, for example, the third Generation Partnership Project (3GPP LTE), worldwide interoperability for microwave access (WiMAX), and the wireless world initiative new radio (WINNER) [3]. These techniques provide orthogonality between the users, reduce interference and improve the network Quality of Service (QoS). In addition, to make the network design process time-efficient, Self-Organizing Network (SON) functionalities added within LTE architecture by incorporating automated optimization, can significantly reduce deployment and maintenance costs (CAPEX and OPEX for CApital Expenditure and OPerating Expenditure respectively). In a wireless network with several cells, the main key to improve the achievable average throughput by user is to mitigate the inter-cell interference caused by using the same frequency within adjacent cells. Various frequency reuse schemes have been proposed in literature [1, 2]. Mitigation technique is generally categorized into three major techniques as shown in [3]: interference cancellation, interference averaging and interference avoidance techniques. The focus in this paper is on avoidance through inter-cell coordination, to achieve better network performance goals [3, 4, 5]. Resource allocation in radio networks essentially depends on the quality of some reference signals received by the User Equipment (UE). In LTE, they are the Reference Signal Received Power (RSRP) and the Reference Signal Received Quality (RSRQ) corresponding respectively to Received Signal Code Power (RSCP) and E\text{c}/N\text{o} in UMTS. Each user is assigned a portion of the spectrum depending on RSRP and RSRQ. The more complex optimization of reference signal is the RSRQ which is based on Signal to Interference plus Noise Ratio (SINR) [2, 6]. SINR is an important performance indicator for estimating the achievable throughput, taking into account the interference received from the neighboring cluster of first-tier cells. The estimation and optimization of the SINR are well-known problems in radio communication systems such as 802.11, GSM or UMTS [11, 12, 13], and LTE needs also a good estimation and control of SINR.

Optimizing antenna parameters configuration to meet variant of service and performance requirement is one of main targets of next generation networks. It can significantly improve the coverage and the capacity of the network dealing with the lack of available bandwidth in base stations. Several studies have been done in this direction to understand the impact of parameters on antenna quality of service offered by the network [6, 7, 14].
Dinan and A. Kurochkin have measured [14] the impact of azimuth and tilt inaccuracies on network performance considering three main quality parameters: service coverage, soft handover areas and the ratio of chip energy to interference Ec/No. The optimization tool used to improve the group of KPIs (Key Performance Indicators) cited above is the recursive optimization algorithm [14]. Many simulation results show that azimuth error in the range of ±8 degrees is tolerable to improve the performance of 42 sites network scenario. Tilt parameter has the same effect on Network performance while setting tolerance is just about ±0.5 degrees. The approach of simulated annealing is used in [7] to study number of network configuration parameters (CPICH power, mechanical downtilt, electrical downtilt and antenna azimuth) effects toward coverage service in UMTS network. The case study demonstrates how the automated optimization can offer a significant performance gain like power consumption of common channels which is a strong indication of reducing the interference in the network. In modern communication systems, further parameters investigations have been developed to meet requirement set. Various combinations of antenna have been studied in term of SINR and throughpout performance in LTE case, outlined for example in [6, 15]. This paper is organized in two main parts: in the first part, we evaluate the Interference model based on SINR for both reuse 1 and 3. The SINR will include a new parameter compared to the classical model. Our contribution on this part consists on adding the load factor of cells to measure the impact of the traffic on the interference model. In the second part, we study the influence of the frequency and the tilt parameters on some performance metrics (quality of the SINR, users in outage...) and also emphasize the interest of robust optimization considering both frequency and tilt as important design parameters when tuning live network. The choice of the robust approach is mainly due to the uncertainty of the traffic distribution due to the traffic change. For this aim, the paper is structured as follows. Section 2 introduces the system model and basic assumptions. Section 3 extends this work and shows the performance metrics and test assumptions. Subsequently, section 4 describes the algorithms and section 5 presents some results to highlight the use of SINR interference model and shows the utility of robust optimization toward the change on the traffic demand. Conclusion and perspectives are drawn in section 6.

2. SYSTEM MODEL
2.1 Basic Assumptions
In this paper we consider the downlink transmission and illustrate the interference schemes using a theoretical model of seven-cell hexagonal layout as shown in Figure 1.

![Figure 1. Seven-cell hexagonal layout. a) 1x3x1 b) 1x3x3](image)

Three sectors are considered in each site with three base stations. In (a) we see the frequency reuse 1x3x1 pattern where 1 site with 3 sectors use 1 frequency set, that is the same frequency set for all sectors. In (b) we see the frequency reuse 1x3x3 pattern where 1 site with 3 sectors use 3 frequency sets, that is different frequency set for all sectors. The 1x3x3 requires a frequency plan but should avoid interference when the network load becomes too high to apply the 1x3x1 pattern. The features of our computational model are the following:

1. Intra-frequency interference is avoided due to the use of OFDMA technique in downlink transmission. In LTE the orthogonality between subcarriers insures that the interference inside the cell can be ignored.

2. The basic resource element in OFDMA is the physical resource block (PRB) which spans both frequency and time dimensions. In this paper, we do not take into account PRB to estimate the inter-cell interference; we only focus on the frequency sub-band reuse scheme. Two adjacent cells are scrambling each other if they are using the same sub-band to transmit data. It gives a worst but fast estimation of SINR.

3. Scenarios are used to represent the traffic distribution of our model since LTE network traffic is unpredictable now. The interference model defined here and based on SINR depends not only on antenna parameters (frequency, tilt, azimuth...) but also on traffic load along day; then in our computation the users available in target sector or adjacent sectors can affect the received signal from other users. As we consider that all users communicate at the same time, a scenario shows the distribution of demand at a given time.

4. We introduce a performance indicator to measure occupancy rate on each sector, the load factor. This indicator is a ratio between used bandwidth and the maximum available bandwidth. It is measured for each sector of the network. The feature of the load factor is to determine the bottlenecks of the network and the overloaded sectors. This indicator will be used in the interference model.

2.2 Case Study and Problem Formulation
The considered network for this study consists of tri-sectors sites in the city of Belfort, located in the north-eastern of France. It is a 40km x 20km area with a lot of big industrial companies and the population is about 200,000 people, that includes inhabitants and people coming from outside the area for work. For our model the service area is divided into a grid of equally sized test points. A test point is a 25x25 meters area.

Due to the very small size of the test point, we assume the same signal propagation conditions within a test point; it means that all users located inside a test point have the same signal and the same RSRP, SINR and RSRQ. Thus, a test point determines the resolution of the computation and the amount of data on signals. A test point is characterized by its number of users and the category of required services for each user (voice, data...). Each sector in the network is equipped with one directive antenna. Each antenna is characterized by its parameters: radiation pattern, azimuth, electrical and mechanical tilts, gain in transmission and reception, frequency and output power in downlink. Due to the dynamic aspect of the network and changes in traffic demand, we introduce the concept of traffic scenarios. A scenario is a given distribution and load of the traffic demand at a given time for each test point of the map. Then, several scenarios allow us to
compute different situations of network performance to study the robustness problem.

The problem formulation is given by the following sets of data, parameters and functions.

Let: $B = \{1, \ldots, n^B\}$, the set of $n^B$ base stations eNB of the network; $T = \{1, \ldots, n^T\}$, the set of $n^T$ test points of the map; and $C_{nt}$, the number of users located on the test point $t$ in scenario $s$.

The interference model based on SINR is thus calculated as defined in Equation 1:

$$\gamma_{b,t,s} = \frac{p_{b,t}^E f_b}{\sum_{b',s} p_{b',t}^R f_{b'} S_{b,s} - n_0 w} \quad (1)$$

Where, $\gamma_{b,t,s}$ is the SINR received by the test point $t$ and issued from the eNB $b$ in scenario $s$; $f_b$ and $f_{b'}$ are the frequencies used by eNB $b$ and $b'$ respectively; $S_{b,s}$ and $S_{b,s'}$ are load factors that corresponds to base stations $b$ and $b'$ in scenario $s$ (load factors are multiplied because we assume that the interference is proportional to the number of users using the same frequency in the target and neighbors cells). Base station $b$ is said to be saturated in scenario $s$ if its load factor $S_{b,s}$ is equal to 1. The term $w$ represents the total bandwidth used by $b$ and $n_0$ is the thermal noise over the bandwidth $w$. The terms $p_{b,t}^R$ and $p_{b,t}^E$ are the end power received by UE located in test point $t$ from respectively $b$ and $b'$. The estimation of this power is given by the Hata propagation model in Equation 2:

$$p_{b,t}^R (\text{dBm}) = p_b^E - PL_{b,t} + S_b^\text{MAX} - a_b^\text{VER} (\theta_{b,t} - t_b^M - t_b^E) - a_b^\text{HOR} (\phi_{b,t} - a_b^\phi) \quad (2)$$

Where, $p_b^E$ is the power in dBm issued from the eNB $b$. $S_b^\text{MAX}$ is the antenna gain while $a_b^\text{VER}$ and $a_b^\text{HOR}$ are the vertical and horizontal radiation pattern due to the position of the test point from the main beam of the antenna. As shown in Figure 2 (a), $a_b^\text{VER}$ depends essentially on the antenna tilt which is the angle of the main beam below the horizontal plane. We distinguish two different tilts: the mechanical tilt $t_b^M$ to adjust the physical angle of the antenna brackets and the electrical tilt $t_b^E$ which does not change the physical angle, but adjusts the radiating currents in the antenna elements to lower the beam in all horizontal directions. The right part of Figure 2 shows the impact of azimuth parameter on the horizontal radiation pattern. Th azimuth is the horizontal angle $\theta_b$ between the north and the antenna main lobe direction.

In 3GPP LTE tests, we apply the two formulas [6] given by Equation 3 and Equation 4 for the computation of $a_b^\text{VER} (\theta_{b,t}, t_b^M, t_b^E)$ and $a_b^\text{HOR} (\phi_{b,t}, \theta_b)$:

$$a_b^\text{VER} (\theta_{b,t}, t_b^M, t_b^E) = -\min \left[ \frac{\theta_{b,t} - t_b^M - t_b^E}{\theta_{b,t}} \right] S_{b,t}, S_{b,t} = 20 \text{dB} \quad (3)$$

$$a_b^\text{HOR} (\phi_{b,t}, \theta_b) = -\min \left[ \frac{\phi_{b,t} - \theta_b}{\phi_{b,t}} \right] A_{\phi}, A_{\phi} = 25 \text{dB} \quad (4)$$

Where, $S_{b,t}$ is the side lobe attenuation and $A_{\phi}$ is the front-to-back attenuation [10]. $\theta_{b,t}$ and $\phi_{b,t}$ are the half power beam width in vertical and horizontal plan respectively.

Finally, with the path loss the Hata model for urban areas is formulated as in Equation 5 [16]:

$$PL_{b,t} = 69.55 + 26.16 \log(f_0) - 13.82 \log(z_b) - a(z_t) + (44.9 - 6.55 \log(z_t)) \log(d_{b,t}) \quad (5)$$

And for small or medium sized city the value of $a(z_t)$ is:

$$a(z_t) = 0.8 + 1.1 \log(f_0) - 0.7z_t - 1.56 \log(f_0)$$

Where, $PL_{b,t}$ is the path loss (dB) in urban area between the eNB $b$ and the test point $t$, $f_0$ is the frequency (Mhz), $z_b$ and $z_t$ are the height of the base station $b$ and the test point $t$ (m), $d_{b,t}$ is the distance between the base station $b$ and the center of the test point $t$ (m), while $a(z_t)$ is the correction factor for mobile unit antenna height (dB).

In the current work, we will consider two parameter settings of the antenna. The study focuses on the impact of the frequency and the tilt parameters on the number of non covered users in the service area. The robust approach uses the mean robustness over three different demand scenarios in a traffic day. The proposed evaluation methodology aims to show the effect of the antenna parameters on the coverage performance metric, with respect to traffic distribution. For the study presented in this paper, the formulation of the overall problem is done in the following.

2.2.1 Decision variables (parameter settings)

$t_b$ is the tilt orientation of the eNB $b$: $t_b \in T_b$

Where $T_b$ is the set of possible values of the tilt parameter.

$f_{b,n}$ is the variable for carrier assignment to eNB : $f_{b,n} \in \{0, 1\}$

$$f_{b,n} = \begin{cases} 1 & \text{if carrier } n \text{ is assigned to eNB } b \\ 0 & \text{otherwise} \end{cases}$$

2.2.2 Constraints

The main constraints of our model are:

(C1) $\forall b \in B$, $V_b^{MIN} \leq V_b \leq V_b^{MAX}$ : minimum and maximum number of neighborhood cells for $b$. $|V_b|$ is the cardinal of neighborhood cells for $b$.

(C2) $\forall t \in T$, $\sum_{b \in B} u_{b,t} \leq 1$ : a test point is associated with exactly one eNB. Where

$$u_{b,t} = \begin{cases} 1 & \text{if test point } t \text{ is associated to the eNB } b \\ 0 & \text{otherwise} \end{cases}$$

Figure 2. Horizontal and vertical angles
Where,

2.2.3  **Fitness function**
Let \( n_{0,s} \) be the number of non-covered users in scenario \( s \).
\[
    n_{0,s}^C = \sum_{i \in s} n_{i,s}^C
\]
where, \( n_{i,s}^C \) is the number of non-covered users in test point \( i \) for scenario \( s \).

2.2.4  **Robustness function**
\[
    f^{Rob} = \sum_{i \in S} n_{i,s}^C
\]
where, \( f^{Rob} \) is the sum of non-covered users in all scenarios.

3. TEST ASUMPTIONS AND PERFORMANCE METRICS
The main parameters and assumptions we used are those selected by 3GPP for LTE as shown in Table 1. Evaluations are performed by a static snapshot of the network level.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Simulation setting</th>
</tr>
</thead>
<tbody>
<tr>
<td>Network layout</td>
<td>35 sites and 88 sectors</td>
</tr>
<tr>
<td>Required service/user</td>
<td>2Mbps</td>
</tr>
<tr>
<td>System frequency</td>
<td>1800 Mhz</td>
</tr>
<tr>
<td>System bandwidth</td>
<td>20 MHz</td>
</tr>
<tr>
<td>Frequency reuse factor</td>
<td>1x3x1 and 1x3x3</td>
</tr>
<tr>
<td>eNB heights range</td>
<td>[17m, 46m]</td>
</tr>
<tr>
<td>UE height</td>
<td>1.5 m</td>
</tr>
<tr>
<td>Propagation loss model</td>
<td>Hata model [16]</td>
</tr>
<tr>
<td>TX power range</td>
<td>[39 dBm, 46 dBm]</td>
</tr>
<tr>
<td>Mechanical tilt range</td>
<td>[0°, 6°]</td>
</tr>
<tr>
<td>Electrical tilt range</td>
<td>[0°, 10°]</td>
</tr>
<tr>
<td>Azimuth range</td>
<td>[0°, 360°]</td>
</tr>
<tr>
<td>Horizontal HPBW</td>
<td>+70°</td>
</tr>
<tr>
<td>Vertical HPBW</td>
<td>+10°</td>
</tr>
<tr>
<td>Antenna gain range</td>
<td>[14dB, 18.9dB]</td>
</tr>
<tr>
<td>Traffic distribution</td>
<td>Distribution in proportion to UMTS traffic load</td>
</tr>
</tbody>
</table>

In addition to Table 1, further assumptions are used for robust optimization tests

1. Three realistic traffic scenarios are tested (8am, 3pm and 6pm)
2. Frequency scheme reuse 3 is retained
3. Deterministic allocation of sub-bands as showed in the right part of Figure 1 is now used
4. The antennas are grouped by site and stored on the basis of an index in ascending order of the x-axis

Various performance metrics are considered herein:

3.1  **Signal to Interference plus noise ratio**
The SINR, expressed in Equation 1, is an important indicator to evaluate cellular networks. SINR choice is motivated by the fact that:

1. It takes into account all the parameters of the antenna.
2. It depends on the traffic distribution and the load factor of the network.
3. It resizes the network and determines which base station controls each user.
4. It allows us to estimate the total throughput of the network.

3.2  **Load Factor**
The Load Factor of the sector/cell is the ratio between the total allocated bandwidth to the cell, that is the required bandwidth and the maximum total bandwidth available in the cell, that is the resources allocated to the cell. Let \( \delta_{b,s} \) be the load factor, then:
\[
    \delta_{b,s} = \frac{w^b_s}{W}\text{ where, } w^b_s \text{ is the total allocated bandwidth to the base station } b \text{ in the reference scenario } s \text{ and } W \text{ is its maximum available bandwidth. It is worthwhile to mention that load factor is one of the main key indicators in cellular networks. It has been suggested that the downlink cell load for a stable network should not exceed 70% [7]. Huge loaded cells are those for which } \delta_{b,s} > 0.7 \text{ and overloaded cells are those for which } \delta_{b,s} > 1.
\]

4. ALGORITHMS
In order to show the interest of robust optimization, we present an algorithm able to quickly find a good solution (the greedy algorithm aims at improving the rate of non uncovered users on the total number of users dropped initially in the network). We were not looking for the best solution at this stage. An iterative algorithm is used; the purpose is not to find an optimal solution but to get the benefit of robust optimization for 3 scenarios in comparison with local solution based on a single scenario. The algorithm with several variants is proposed for each parameter: frequency allocation and tilt configuration. We measure the effect of each parameter toward the network coverage metric.

4.1  **Frequency parameter optimization**
It can be proved that frequency assignment problem is NP-hard as it is a graph-coloring problem. For such problems, guaranteeing optimum requires, in the worst case, an enumeration of all possible configurations. The number of possibilities is enormous; in our case study, for 35 cells, 88 antennas and 3 frequency groups, the number of possibilities is \( 6^{35} = 1.71 \times 10^{27} \). The robust optimization function takes into account the three scenarios considered above. The used algorithm is described in the following. We run the optimization with different varying conditions:

1. The scenarios of traffic: several traffic hours.
2. The procedure for the initial frequency assignment to the base stations: deterministic or stochastic per sector from the same site.
3. The sites neighborhood search to test the permutation of frequency: sites ranked from the input file or randomly chosen during optimization.

The algorithm starts with one solution using the reuse scheme 1x3x3. The optimization algorithm is run for each scenario to show the best configuration of the frequency parameter setting with respect to the performance metric given by the Equation 6.
For each explored site, we evaluate the 6 (3! =6) possibilities of permutations for each sector of the site. The algorithm evaluates 6x88 permutations at each iteration. If a frequency permutation improves the evaluation function of the current solution, the algorithm keeps the last modification and goes through the next sector configuration. The algorithm stops once the current iteration brings no improvement. This is achieved by the following algorithm which was used for all cases.

**Algorithm for frequency optimization**

**Input parameters**

Set B of n base stations; Set T of n test points; Set S of scenarios:

- s1=8am,
- s2=3pm
- s3=6pm

Sentence: Frequency reuse scheme 1x3x3 (3 groups of frequency to assign to base station)

**Variables**

- Frequency assignment to base stations
- Fitness function

Fitness(F) = Number of outage users for the frequency plan F

in s for non robust optimization

in s1, s2 and s3 for robust optimization

**Algorithm**

1. Initialize F // F is the initial frequency plan
2. \( F^* = F // F^* \) is the current best frequency plan
3. Repeat
   1. Improve=False
   2. For each site b of the network // Testing all the sites
      1. For each permutation j=1:6 // Testing all the permutations of frequency on b
         1. Generate the new frequency plan F from \( F^* \)
         2. IF Fitness(F)<Fitness(\( F^* \)) // Evaluation of the current configuration
            1. \( F^* = F // Store the new best solution of frequency plan \)
            2. Improve=True
       End IF
   End For
   End For
4. Until Improve=False // Stopping criteria if there is no improvement,

**Algorithm for tilt optimization**

**Input parameters**

Set B of n base stations; Set T of n test points; Set S of scenarios:

- s1=8am,
- s2=3pm
- s3=6pm

Sentence: Tilts in operation

**Variables**

- Tilt orientation of the base stations
- Fitness function

Fitness(T) = Number of outage users for the tilt configuration T

in s for non robust optimization

in s1, s2 and s3 for robust optimization

**Algorithm**

1. Initialize T // T is the initial Tilt configuration
2. \( T^* = T // T^* \) is the current best frequency plan
3. Repeat
   1. Improve=False
   2. For each antenna b of the network // Testing all the antenna
      1. For each configuration j=0:12 // Testing all the tilt configurations on b
         1. Generate the new tilt configuration T from \( T^* \)
         2. IF Fitness(T)<Fitness(\( T^* \)) // Evaluation of the current configuration
            1. \( T^* = T // Store the new best solution of tilt configuration \)
            2. Improve=True
       End IF
   End For
   End For
4. Until Improve=False // Stopping criteria if there is no improvement,
we estimate again the load factor for each station. This second step is repeated several times (10 times) to try to reach a stable network configuration.

The collected traffic data come from a real UMTS network. The tests consider three different scenarios originating from the traffic of one day, as shown in Figure 3. Three scenarios were selected at different times of the day as follows: a first scenario at 8am with low traffic and 482 users dropped randomly in the network; a second scenario at 3pm with medium traffic and 1,019 users; and a third scenario at 6pm with high traffic and 1,471 users. We are considering that all users are accessing the network at the same time (saturated traffic condition).

**Figure 3. Example of day traffic with three chosen scenarios**

Figure 4 shows the concentration of the traffic in the 3rd scenario at 6pm (high traffic). The traffic is represented by a color gradient. The light color shows a low traffic, while the dark color shows higher traffic.

![Traffic Concentration at 6pm](image)

**Figure 4. Example of traffic concentration at 6pm**

### 5.1 Interference model results

To compare the performances of both reuse 1x3x1 and reuse 1x3x3 patterns, the number of users in outage is used as a performance metric. The minimum required SINR is equal to 0.9 dB [8]. Below this value of SINR, one user cannot establish a communication as defined in Equation 8:

\[
\gamma_{b,t,s} = \frac{p_{b,t}^R \delta_{b,t} \delta_{b',s} + n_{b,t}^N}{\sum_{b'=h}^{R} p_{b',t}^R \delta_{b',t} \delta_{b',s}} < \gamma_{MIN} \quad (8)
\]

where \(\gamma_{MIN}\) is the required threshold.

Figure 5 depicts the number of users in outage obtained with both reuse patterns: scheme 1x3x1 (abbreviated scheme 1 in Figure 5) and scheme 1x3x3 or simply scheme 3 (Figure 5). In the network design we test for scheme 1x3x3, the sub-band assignment depends on the azimuth orientation of the sectors. Sectors in opposite direction from neighbor sites are assigned different frequency groups. The program implementing our model is developed in C++. We run the program ten times at least to get stable results (as there is a random process in the system computation); an example of three scenarios of traffic is presented in the following (Figure 5) to show the interest of using the reuse scheme 1x3x3 in a real network design and traffic load.

![Reuse Scheme Comparison](image)

**Figure 5. Reuse scheme 1 and scheme 3 results with 3 scenarios**

We remind that the frequency reuse 1 (or 1x3x1) scheme whereby the whole available bandwidth is used in each cell/sector and the frequency reuse 3 (also called 1x3x3) scheme in which the entire bandwidth is divided into 3 non-overlapping groups and assigned to 3 co-site sectors within each cell.

In Figure 5 we see that the number of users in outage is more important in scheme 1x3x1 (13, 36, and 40) than in scheme 1x3x3 (8, 18 and 17) for the three scenarios of traffic load considered here (8am, 3pm and 6pm respectively). These results are consistent since the total bandwidth used in pattern 1 can assign more resources, but would jeopardize the rate offered by the network. This is due mainly to the undesirable inter-cell interference generated by neighboring cells using the same frequency set. Such a dense reuse is an obvious pitfall which limits the throughput at the cell edge. We can also note according to these results that, the higher the traffic, the higher the number of outage users, whatever the frequency pattern solution.

### 5.2 Frequency and tilt optimization

The second part of this study is dedicated to robust optimization. It shows that optimizing a number of network configuration parameters like antenna frequency and tilt orientation helps considerably to meet variant of performance requirements. A greedy algorithm is used to examine how the solution of the antenna configuration, behaves under realistic scenarios.

#### 5.2.1 Results with non robust and robust optimization

#### 5.2.1.1 Frequency optimization results

The results of optimization are shown in the Figures 6 and 7. We emphasize that for the non robust (each scenario tackled alone) and for the robust optimization (all scenarios together) we use the same algorithm but in case of robustness the evaluation function is the Equation 7 and takes into account the configuration of the frequency considering all the scenarios simultaneously. It means that, for each frequency of the network, we evaluate the non-covered users in the three scenarios. So, we run the same algorithm 4 times (one run for each optimization), we use the evaluation function Equation 6 to optimize the 3 scenarios separately; then we use the evaluation function (Equation 7) for the robust optimization using the 3 scenarios at the same time.
optimization in Test 2 and Test 3, and keep the best solution for several parameters. We run the program 20 minutes for each input file.

Different variants of the algorithm have been tested by varying the robust approach is important for the remaining of this study.

Test 1 (Figure 6): the initial frequency plan is deterministically assigned and the sites are processed respecting their rank in the input file. The x-axis represents the starting solution and the optimization of scenarios $s_1$, $s_2$ and $s_3$ separately and the robust optimization at the end. The y-axis shows the number of users in outage for each scenario $s_1$, $s_2$, $s_3$ and total number. We can note that scenario $s_1$ optimization has the smallest number of non-covered users when evaluating $s_1$ (4 users) comparing to the other cases (8, 7, 9). The same analysis can be done for the scenario $s_2$ and it is different for $s_3$ but not far away from the best one. After 20mn of run there is no guarantee on the solution quality. We observe that the result of the robust optimization is a tradeoff between the three scenarios, the best for $s_1$ and $s_2$ but not the best for $s_3$. Finally, the fitness function value of non-covered users for all cases corresponds to the global solution (blue color in the right part), while in other situations, starting solution and non robust cases, the global function values are 43, 25, 27 and 29 respectively from left to right part of the Figure 6. The robust optimization does a better compromise between all scenarios. This result shows how the robust approach is important for the remaining of this study. Different variants of the algorithm have been tested by varying several parameters. We run the program 20 minutes for each optimization in Test 2 and Test 3, and keep the best solution for the considered fitness function.

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Test 2 (Figure 7): the initial frequency plan is deterministically assigned and the sites are processed respecting their rank in the input file. The x-axis represents the starting solution and the optimization of scenarios $s_1$, $s_2$ and $s_3$ separately and the robust optimization at the end. The y-axis shows the number of users in outage for each scenario $s_1$, $s_2$, $s_3$ and total number. We can note that scenario $s_1$ optimization has the smallest number of non-covered users when evaluating $s_1$ (4 users) comparing to the other cases (8, 7, 9). The same analysis can be done for the scenario $s_2$ and it is different for $s_3$ but not far away from the best one. After 20mn of run there is no guarantee on the solution quality. We observe that the result of the robust optimization is a tradeoff between the three scenarios, the best for $s_1$ and $s_2$ but not the best for $s_3$. Finally, the fitness function value of non-covered users for all cases corresponds to the global solution (blue color in the right part), while in other situations, starting solution and non robust cases, the global function values are 43, 25, 27 and 29 respectively from left to right part of the Figure 6. The robust optimization does a better compromise between all scenarios. This result shows how the robust approach is important for the remaining of this study. Different variants of the algorithm have been tested by varying several parameters. We run the program 20 minutes for each optimization in Test 2 and Test 3, and keep the best solution for the considered fitness function.

Test 3 (Figure 7): the initial frequency plan is randomly assigned to the co-site sectors and the sites are randomly processed during optimization.

Figure 8 shows 5 parts, from the right to left: starting solution, optimization of scenarios $s_1$, $s_2$ and $s_3$ separately, and then robust optimization. The starting point of the algorithm is the starting solution (43, 8, 18 and 17) which represents the number non covered users in the global function (Equation 7) and scenario function (Equation 6) for each scenario.

5.2.1.2 Tilt optimization results
Robust optimization results for the tilt parameter are highlighted in the right part of each test (Figure 8 and 9). Several tests have been made to show the tilt parameter effect on the number of non covered users, we limit at showing 2 tests varying the neighborhood sites process and the stopping criteria.

Test 1 (Figure 8): the algorithm presented on 4.2 is implemented. It means that with the same starting solution (3 scenarios of traffic and the operating tilts in real network), the site neighborhood search is done according their storage in the data file. In addition of sites search, the algorithm stops once there is no improvement of the solution. Results are shown in Figure 8.

Figure 8 shows 5 parts, from the right to left: starting solution, optimization of scenarios $s_1$, $s_2$ and $s_3$ separately, and then robust optimization. The starting point of the algorithm is the starting solution (43, 8, 18 and 17) which represents the number non covered users in the global function (Equation 7) and scenario function (Equation 6) for each scenario.

We emphasize that the optimization of each scenario provides better results when each scenario is tackled separately (7, 11, 12) respectively, but impacts the global function. In robust optimization, we can easily note that the configuration found by the algorithm is a better compromise between all scenarios, $T_{Rob} = 31$ compared with starting solution and the scenarios optimization (43, 41, 33 and 34).

Figure 9 shows 5 parts, from the right to left: starting solution, optimization of scenarios $s_1$, $s_2$ and $s_3$ separately, and then robust optimization. The starting point of the algorithm is the starting solution (43, 8, 18 and 17) which represents the number non covered users in the global function (Equation 7) and scenario function (Equation 6) for each scenario.

Test 2 (Figure 9): we keep the same initial conditions; but vary the sites neighborhood search (random search) and stopping criteria (an hour of run). It shows the same results as in Figure 8. It confirms that optimizing by means of robust function can improve the network coverage with regard to traffic distribution.
The Figure 10 represents a comparison between the 2 parameter setting optimizations; with the same initial condition (Test 1 in the frequency case and Test 1 in the tilt optimization case).

![Comparison frequency/tilt optimization](image)

**Figure 10.** Comparison between frequency and tilt optimization: Sites processed according their storage in data file; stopping criteria when there is no improvement

According to these results, we note that optimizing the frequency parameter provides better results while taking coverage as a performance indicator: less uncovered user for $s_1$ case (4<7); $s_2$ (8<11) and $s_3$ (9<12) and also in robust optimization (21<31). Such results are expected to happen. This is due mainly to the undesirable inter-cell interference generated by neighboring cells using the same frequency set. It impacts more the SINR quality comparing to the tilt parameter.

### 6. CONCLUSION

In this paper we have shown the interference model and the interest of robust approach with respect to traffic distribution in LTE downlink system. The analysis has been carried out using model radiation pattern and simple model of system performance. The interference model has been validated based on SINR computation and comparing two reuse schemes (1x3x1 and 1x3x3) under realistic scenarios. With respect to coverage, it has been observed that the reference reuse 1x3x3 presents best results with respect to the number of covered users, independently from the traffic demand. It shows also that the load factor could impact the quality of signal at end users. It is an important indicator because it highlights the overloaded cells which represent the bottleneck of the network. Using system simulations, we studied how the frequency and the tilt parameters setting affect the coverage of the macro-cellular scenario. Different combinations of frequencies and tilts are used and obtained results show how coverage indicator is sensitive to the combination, and also to the traffic inaccuracies. Simple algorithms used here confirm the interest of robust approach irrespective of realistic traffic load. As perspectives, we aim in further studies at analyzing the influence of the load factor throughout the capacity performance metric to bring out the overloaded cells which represent the bottlenecks of the network. We will also study the impact of the power transmission parameter on the interference model and other performance metrics (throughput, capacity). Furthermore, robust optimization approaches like the Variable Neighborhood Search and Tabu Search will be studied to highlight the impact of the traffic uncertainty in the deployment of the network.

### 7. REFERENCES


