

SBAS C/A Code Interferences Characterization And Mitigation

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BIOGRAPHY

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ABSTRACT

It is well known that GPS C/A codes present cross correlation peak potentially causing false acquisitions. These cross-correlations peaks can in addition cause tracking errors and C/No degradation [1], [2], [3], [4] and [5], not in traditional GPS tracking situations, but for applications where signals are received with low Doppler.

There are several applications that can have low relative Doppler, and thus more frequent Doppler collision causing code cross-correlation interference : the first application occurs with the use of ranging signal broadcasted from geostationary satellites (SBAS systems) when two or more geostationary satellites are in common views of a fixed or low dynamic receiver (control station, reference station for differential positioning or any ground user with none or little motion), the second application occurs when ground pseudolites are used, with a receiver either on board a geostationary satellite or in a plane and on the ground as well.

The findings described in this paper are part of the work performed by M3 Systems under a project initiated by the

CNES (French Space Agency) which aims at studying the EGNOS RIMS performances.

The work presented here aimed at:

- Characterizing precisely these C/A codes interference tracking errors on WAAS satellites,
- Identifying the exact factors driving the occurrence of these errors

INTRODUCTION

The goal of this study is to show that, when specific conditions are met, large tracking errors can occur with C/A code due to C/A code cross-correlation interference.

The interference mechanism is physically the same than for multipath error. Actually, multipath can be viewed as C/A code interference on itself. For multipath error, the cross correlation peak of the reflected signal adds its contribution to the correlation function and causes an offset of the zero-crossing of the discrimination function. This offset is the tracking error. For C/A code interference, the cross-correlation peak of the interfering code causes the same effect. Normalized cross-correlation peak values are either $+63/1023$ or $-65/1023$. A simple analysis shows that the error can reach up to 18 meter for a half chip spacing correlator. If the cross-correlation function of the desired and interfering codes has a secondary peak that falls within the receiver chip spacing of the relative code offset, there is potential for a tracking error.

A necessary condition for C/A code interference to take place is to have the relative Doppler between the 2 interfering signal lower than the receiver code loop bandwidth that is typically lower than 1 Hz. The reason is that the signed amplitude of the interfering peak is function of the relative phase, and if the relative phase moves too much during the code loop integration period, the interfering peak (and the tracking error) will be filtered. We can name this condition as “Doppler Collision” or as having “quasi-stationary code” because from the receiver point of view, the received codes will not move one relatively to another, the cross-correlation peak of the interfering signal will not move relatively to the main auto-correlation peak of the desired signal, and the interference will result in a lasting bias.

For common GPS application, having a Doppler collision smaller than 1 Hz is quite a rare phenomena: indeed the Doppler due to the satellite motion is high: from -4.5kHz to 4.5kHz for standard use, so there is a low probability to have Doppler collision lower than 1 Hz leading to a tracking errors, and even if it happens, it will only last a few seconds. Therefore, for common GPS applications, C/A code interference rarely leads to a noticeable tracking error.

However, with the development of the Satellite Based Augmentation Systems (SBAS) using geostationary satellite, like EGNOS, WAAS, GAGAN, or MSAS, the dynamics are much lower, in the range of a few 10's of Hz. Doppler collision will happen twice a day and last several minutes and even more. The lower the relative Doppler will be, the longer the interference will be significant. Interference due to C/A code cross-correlation will happen. These C/A code interferences can cause false acquisition, C/No degradation and tracking error. This paper will focus on the tracking error due to the C/A code cross-correlation encountered in real situations using WAAS data collected by EGNOS's Range and Integrity Monitoring Stations (RIMS). It will also show the impact of several factor, including the navigation message on the tracking error. This work is subsequent to previous papers where theoretical cross-correlation tracking error have been already studied [1], [2], [3], [4], [5] and simulated in laboratory [3].

The first section of this paper presents the applications concerned by this phenomenon. The second section introduces theoretical aspect of this interference. The next section shows the real-life identification of the C/A code interference tracking errors, based on WAAS data collected by EGNOS RIMS. Finally, the last section introduces the possible interferences mitigation techniques.

1- APPLICATIONS

A- Geostationary Satellites Motion

Geostationary satellites motion is supposed to be fixed relative to the earth, therefore, signals from SBAS geostationary satellites would always be in Doppler collision with one another when received by a fixed receiver.

In reality, geostationary satellites move slowly within a station-keeping window, mostly along the N-S and the E-W axis, with a 24-hour period. This generates relative Doppler with an harmonic pattern and an amplitude of several 10's of Hz, so Doppler collision inside the code loop ($\sim 1\text{Hz}$) occurs only twice a day during a few minutes (see figures 4 and 5).

B- SBAS Satellites Applications

The first application concerns the ranging signal broadcasted from geostationary satellites, when two or more satellites are in common view of a fixed receiver or with low dynamic (control station, reference station for differential positioning or any ground user not moving).

To resolve integrity problems and to improve GPS performances, the Satellite Based Augmentation System (SBAS) has been developed with different inter-operable regional complements like EGNOS, WAAS, GAGAN, and MSAS, for instance.

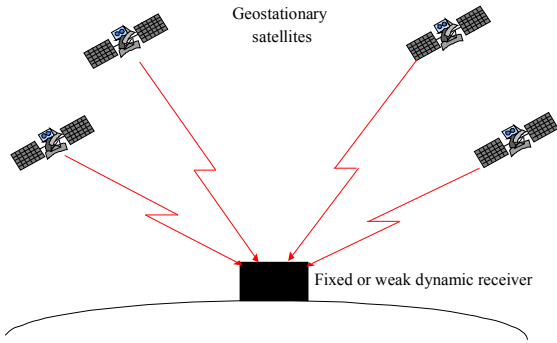


Fig. 1 : SBAS application

A tracking error due to C/A code cross-correlation can occur when at least two geostationary satellites are visible from a fixed receiver and increase strongly with more geostationary satellites. Indeed it is thus possible that all the signals will be interfering at the same time, or sequentially, one after another.

C- Pseudolites

The use of pseudolites can also induce low dynamic signals.

Two applications can involve pseudolites:

- pseudolites and receiver on board geostationary satellite
- pseudolites and fixed or low dynamic receiver

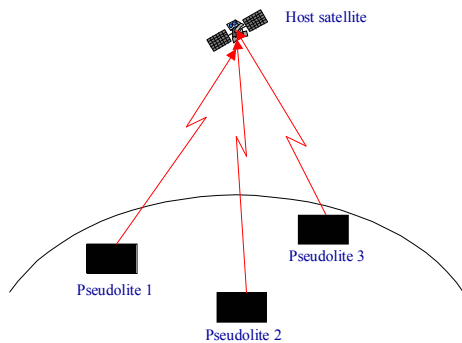


Fig. 2 : Pseudolite application

2- TRACKING ERRORS – THEORY

In presence of interfering signal, the receiver delay lock loop does not track only the desired signal delay but the delay of the sum of the desired signal (index k) and all interfering signals (index 1 to N).

The received signal can thus be written as follows:

$$c_r(t) = \sum_{i=1}^N a_i d_i(t - \tau_i) p_i(t - \tau_i) \cos(\omega t + \varphi_i(t))$$

Where:

$p_i(t)$: PRN code sequence of the i^{th} satellite

$d_i(t)$: Data from the i^{th} satellite

ω : Pulsation of the reference signal

$a_i(t)$, $\tau_i(t)$ and $\varphi_i(t)$: Power, Propagation delay and Phase of the i^{th} signal wrt. the desired one

With an early minus late power code discrimination function and in presence of low Doppler, **the error function** induced by C/A code interference can be written as follows [1]:

$$V_e(\Delta \hat{\tau}_k) = 2 \sum_{i=1}^N a_i a_k \left[R_{k,k}(\Delta \hat{\tau}_k - \frac{T_c}{n}) R_{k,i}(\Delta \hat{\tau}_k - \Delta \tau_{k,i} - \frac{T_c}{n}) \dots \right. \\ \left. R_{k,k}(\Delta \hat{\tau}_k + \frac{T_c}{n}) R_{k,i}(\Delta \hat{\tau}_k - \Delta \tau_{k,i} + \frac{T_c}{n}) \right] \int_{\sqrt{B_n}} d_k(t - \tau_k) d_i(t - \tau_i) \cos(\Delta \varphi_{k,i}(t)) dt + \dots \\ \sum_{i \neq k}^N a_i^2 \left[R_{k,i}^2(\Delta \hat{\tau}_k - \Delta \tau_{k,i} - \frac{T_c}{n}) - R_{k,i}^2(\Delta \hat{\tau}_k - \Delta \tau_{k,i} + \frac{T_c}{n}) \right] \dots \\ 2 \sum_{i \neq k}^{N-1} \sum_{j \neq k}^N a_i a_j \left[R_{k,i}(\Delta \hat{\tau}_k - \Delta \tau_{k,i} - \frac{T_c}{n}) R_{k,j}(\Delta \hat{\tau}_k - \Delta \tau_{k,j} - \frac{T_c}{n}) \dots \right. \\ \left. R_{k,j}(\Delta \hat{\tau}_k - \Delta \tau_{k,j} + \frac{T_c}{n}) R_{k,i}(\Delta \hat{\tau}_k - \Delta \tau_{k,i} + \frac{T_c}{n}) \right] \int_{\sqrt{B_n}} d_i(t - \tau_i) d_j(t - \tau_j) \cos(\Delta \varphi_{i,j}(t)) dt \dots$$

Where:

$R_{k,i}$: Cross-correlation between the desired signal “k” and the i^{th} signal

B_n : Bandwidth of the Delay Lock Loop

T_c : Code C/A period

n : Length of the code C/A

From this mathematical expression we observe that the tracking error induced by C/A code interference will depend on different parameters:

- the relative code delay: $\Delta \tau_{k,i} = \tau_i - \tau_k$
- the power factor : $a_i a_k$
- the relative carrier phase: $\Delta \varphi_{i,k} = \varphi_k - \varphi_i$
- the relative Doppler
- the cross-correlation function: $R_{k,i}$
- and the message data : d_i

3- TRACKING ERRORS - OBSERVATIONS

All the analyzed WAAS data are real data, RINEX format and other receiver raw measurements (C/No, receiver flags) being issued from EGNOS RIMS collected by the

EGNOS PACF (Performance Assessment and Check-out Facility).

A- Detection of the C/A Code Interference

These results are based on the analyze of WAAS data collected by the RIMS station type B of Moncton (Canada) between 2008-03-09 and 2008-03-13 for which the interference error was clearly visible.

The following figure is a map showing the location of the Moncton RIMS B station and the two interfering satellites:

- WAAS satellite PRN 135 (GALAXY 15-PanAmSat)
- and WAAS satellite PRN 138 (ANIK F1R-Telesat)

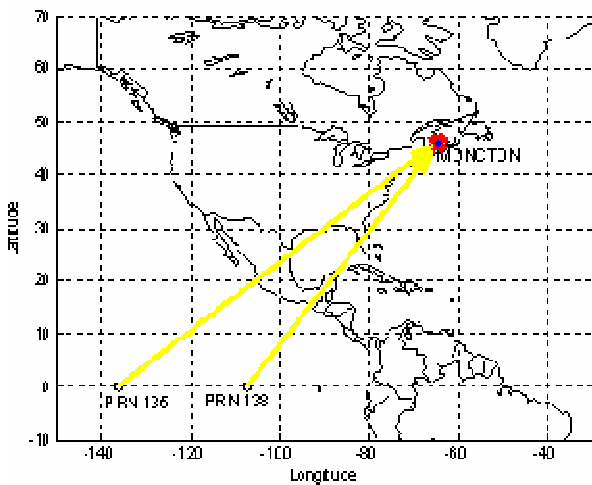


Fig. 3 :MONCTON RIMS Localization

The following figure presents the Doppler evolution and the relative Doppler between geostationary satellites PRN 135 and 138, seen from Moncton:

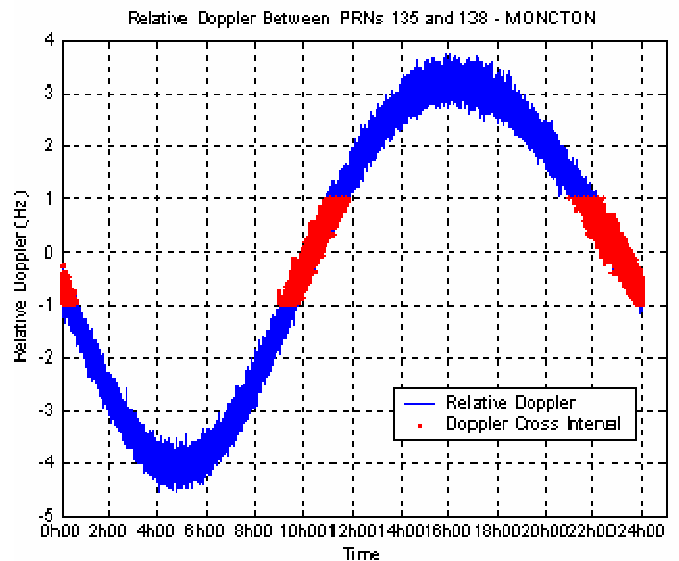
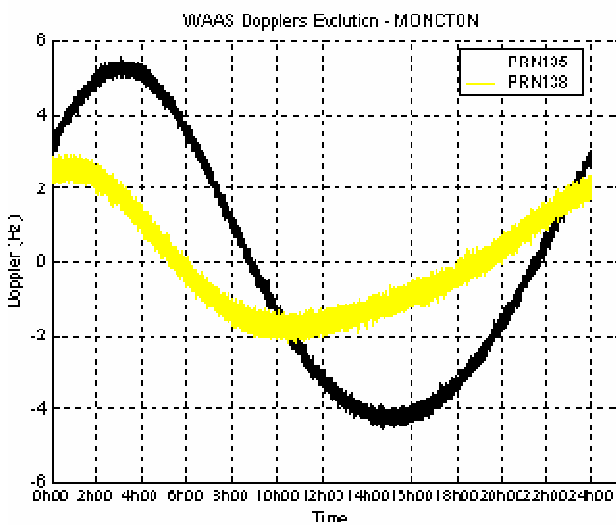


Fig. 4 : Relative Dopplers and Doppler Collisions between geostationary satellites PRN 135 and 138 (Moncton station)

On this figure, we observe two periods of approximately 3 hours (in red in the figure) where the relative Doppler is less than 1 Hz (approx. the code bandwidth) between those 2 WAAS satellites. This implies that, during 6 hours per day (more than 25% of the time), C/A code interference can occur.

B- Characterization of the C/A Code Interference

The characterization of the C/A code interference is made using three complementary methods:

- Computing the 3rd degree derivative of the C1 pseudo distance (code C/A on L1). This allows to have a first estimation of the noise which affects the C1 measurement. The tracking bias is characterized by an increase of the noise.
- Analyzing the residuals errors on C1 measurement obtained by polynomial interpolation of C1 by a 15th order polynomial and a sliding window of 2 hours.
- Analyzing the enabling causes for fine analysis:
 - o Relative Doppler,
 - o Gold sequences cross correlation function,
 - o SBAS navigation messages correlation.

The 3rd Derived of C1 between the 2008-03-09 and the 2008-03-13 shows an increased noise on the measurement of the WAAS PRNs 135 and 138, which only happens during Doppler collisions between these satellites. These noises reach a maximum value at approx. 10h and 23h, as illustrated in the following figure:

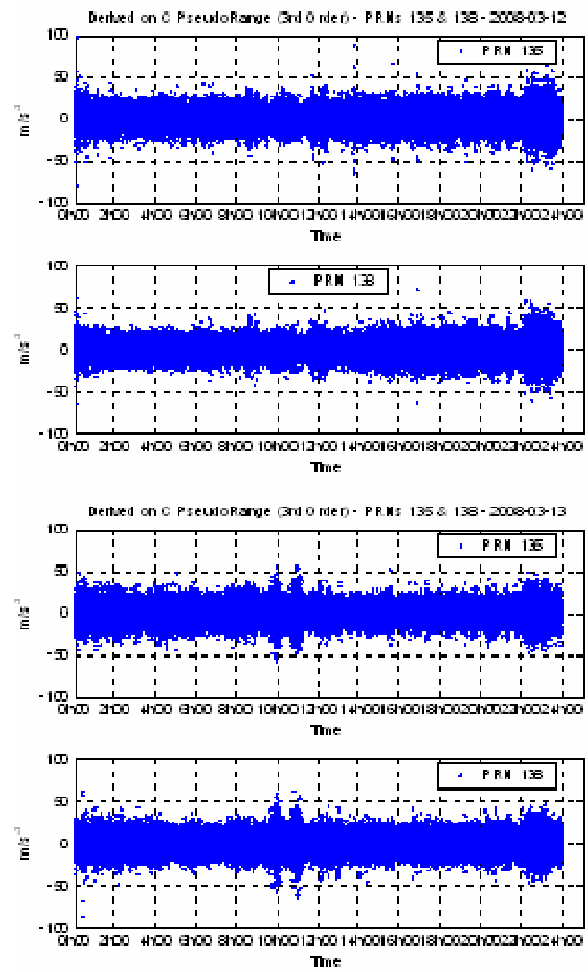
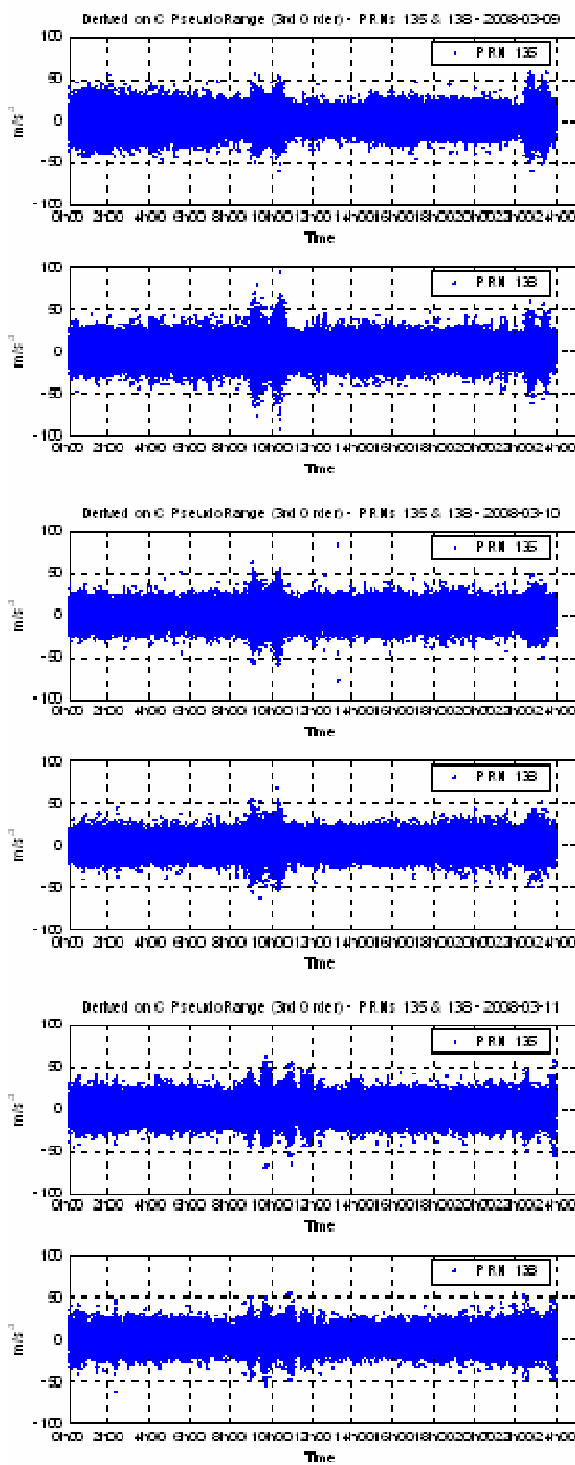


Fig. 5 : 3rd Derived of C1 – PRNs 135 & 138 – Moncton

Analysis of the 1st Doppler collision between 9h-12h (2008-03-09)

Residual values on C1 for PRN 135 and 138 are presented on the next figures:

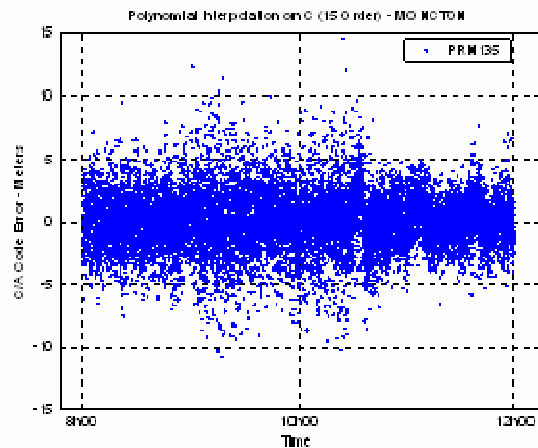


Fig. 6 : Residuals Error on C1 – PRN135 - Moncton

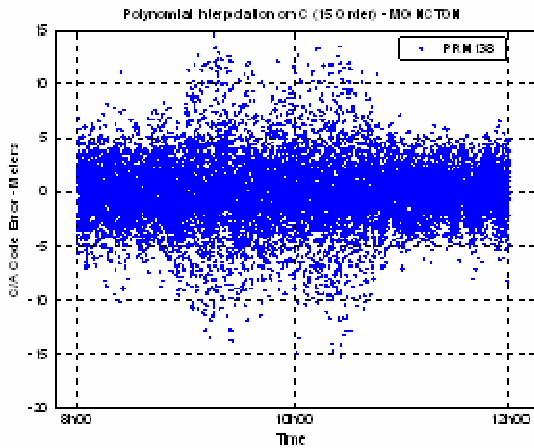


Fig. 7 : Residuals Error on C1 – PRN138 Moncton

These figures show that we have residual errors up to 14 meters on C1 measurements on WAAS PRNs 135 & 138, during the first Doppler collision between these PRNs.

The following figure shows the code relative pseudo-range and the Cross Correlation function of the PRNs sequences during time. We note that between 8h30 and 10h30 the relative chip offset is between 727 and 729 chips, and figure 9 shows that this corresponds to a secondary peak of the X-correlation function.

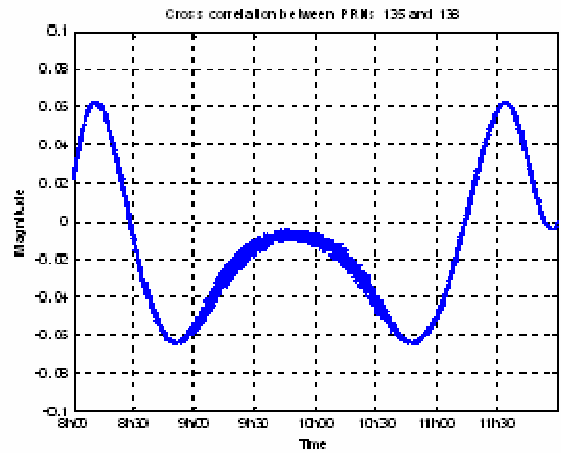
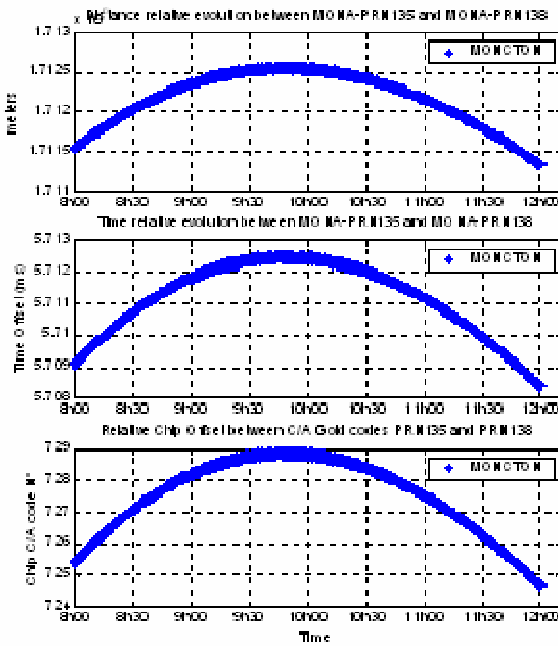


Fig. 8: Relative Distance, Time, Chip Offset and Cross Correlation between PRNs 135 & 138 - 1st Doppler Collision

The following figure is a zoom between 8h30 and 11h00 of the Chip relative offset, Cross Correlation function and cross correlation value for the prompt correlator over time:

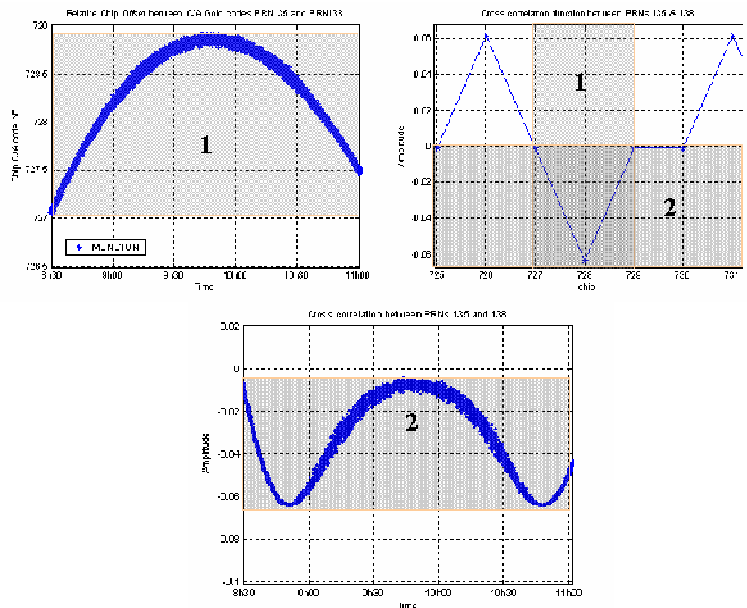


Fig. 9: Cross Correlation functions exact and interpolate during 1st Doppler Collision

RELATIVE POWER

In addition, we note that PRN 135 is received with 2 dB more power than PRN 138 during the first Doppler collision. This explains why the tracking error is larger on PRN 138, the reason is PRN 135 interferes more on PRN 138 than PRN 138 interferes on PRN 135 (fig. 6 & 7).

NAVIGATION MESSAGE

Remark:

The raw navigation message of the SBAS signal contains 500 symbols, transmitted each second. This sequence is the convolutional encoding of the 250 bits of the SBAS navigation message available on the <ftp://serenad-public.cnes.fr>. With the convolution encoder logic described in MOPS DO229C presented below, it is possible to recover the 500 original SBAS symbols.

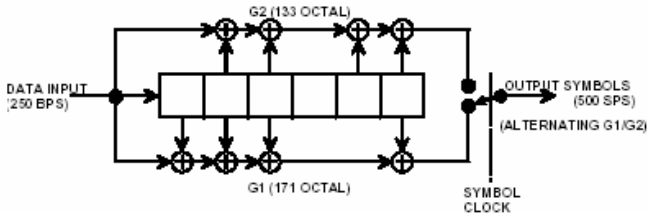


Fig. 10: Convolutional Encoding

If the navigation message symbol sign is reversed, then the sign of the interfering peak will also be reversed. Therefore, for the tracking interference to reach full scale, the navigation symbols of the interfering signal have to be the same.

If this is not the case, then we expect the tracking error to be modulated according to the data message symbol x-correlation function.

Next figure shows the x-correlation computed over 1s data frame for the data symbols coming from PRN 135 and 138:

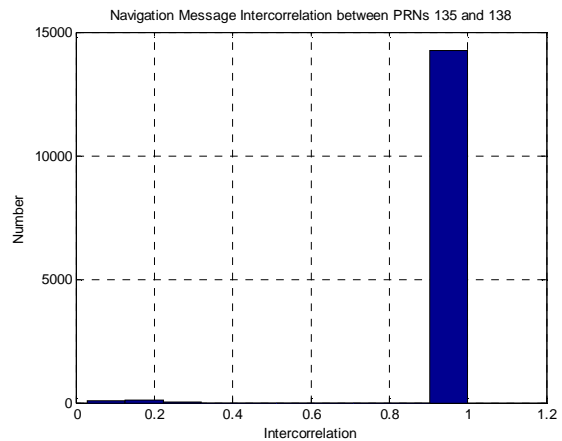
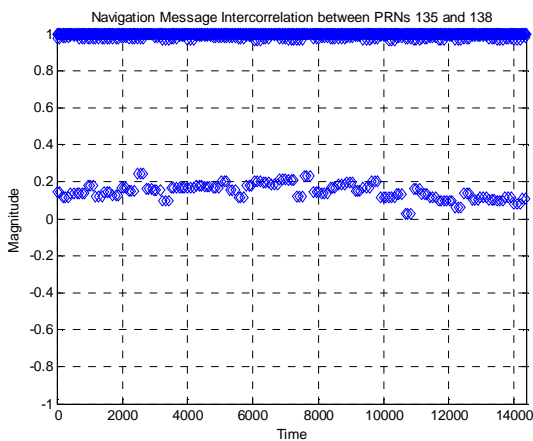


Fig. 11: Navigation messages correlation function and distribution of PRNs 135 and 138

It appears that raw transmitted navigation symbols are strongly correlated between 8h00 and 12h00 (correlation function reaching 0.8 to 1), a 0.8 correlation values means that over a 1s frame, 90% of the data symbols have the same sign, and 10% are of opposite sign).

4- C/A CODE INTERFERENCE MITIGATION

A -Carrier Smoothing

As C/A code interferences looks like multipath, some multipath-like mitigation techniques can be envisaged. But other techniques can not.

Narrow correlator or double delta correlator is a technique that can't be used, because WAAS signals are band limited.

Carrier smoothing can be used to reduce code tracking noise as well as tracking error.

For WAAS end-users, the smoothing of pseudorange observations using integrated carrier phase observations is given by the following equation [5]:

$$\tilde{P}_n = \frac{1}{K} \cdot P_n + \left(\frac{K-1}{K}\right) \cdot \left[\tilde{P}_{n-1} + \left(\frac{\lambda}{2\pi}\right) \cdot (\phi_n - \phi_{n-1}) \right] \quad (\text{eq. 1})$$

Where:

- P_n is the raw pseudorange,
- \tilde{P}_n is the smoothed raw pseudorange,
- Φ_n is the phase measurement in radian,
- λ is the wavelength,
- K is the filter parameter (time constant).

The following figures show the residual errors on the C1 measurements for different carrier smoothing time: 20 and 100 seconds (as recommended in [6]) for PRNs 135 & 138 on Moncton RIMS station.

For PRN 135, with carrier smoothing of 20 seconds, we observed that the C/A code interference errors have been reduced by a factor 5 approximately to reach maximum values about 3 meters.

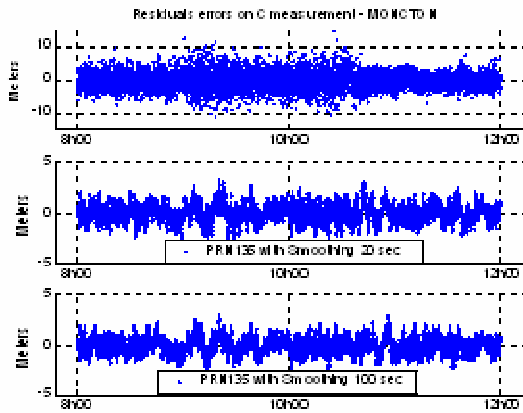


Fig. 12 : Residuals Error on C1 with Carrier Smoothing of 20 and 100 seconds on PRN135

The same behavior is observed for PRN 138; with carrier smoothing of 20 seconds, we note that the C/A code interference errors have been reduced by a factor 5 approximately to reach maximum values about 3 meters.

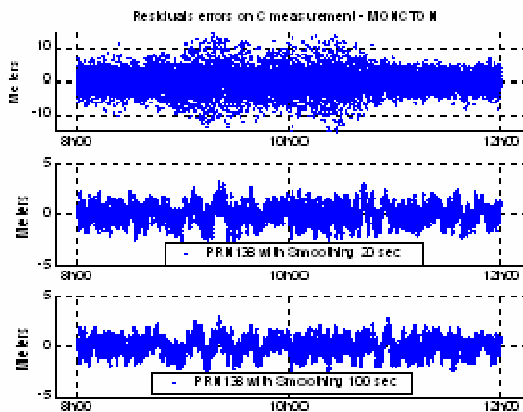


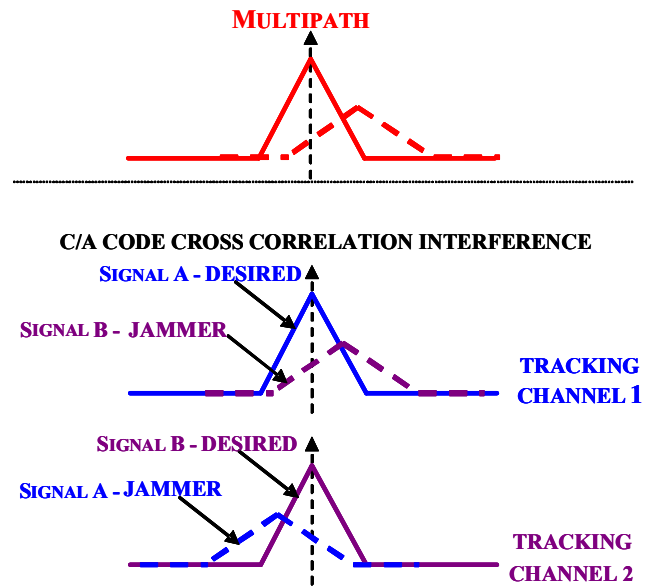
Fig. 13 : Residuals Error on C1 with Carrier Smoothing of 20 and 100 seconds on PRN138

As we can see, applying a carrier smoothing on 100 seconds, as recommended by MOPS [6], gives good results in terms of C/A code interference mitigation. The remaining oscillations on the smoothed pseudorange residuals could be due to multipath and/or residual errors in the code/carrier coherency (fig. 12 & 13).

B- C/A Code Interference Correction Algorithm

Fortunately, mutual C/A code interferences have an interesting difference wrt multipath: if the receiver tracks all the signals in view, we can assume that the interfering

signal is tracked on another receiver channel, and is therefore observable.



	Tracked Code	Interfering Code
Channel A	Code 1	Code 2
Channel B	Code 2	Code 1

Table 1: Correction algorithm principle

The idea is to let the receiver track each signal. The correction comes as a post processing on the raw measurements.

The receiver provides code delay, phase, power, Doppler and data for each satellites and knowing the cross-correlation function for each code pair, it is possible to predict the tracking error and then to subtract it from the raw code pseudo-range measurements. This has been demonstrated with simulated signals (same data symbols) coming from a Spirent Simulator in [3] and [4].

Results with this C/A code interference correction algorithm, using real data, will be presented in forthcoming publications.

CONCLUSION

Analysis of real GNSS data collected by EGNOS RIMS allowed to highlight that C/A code interference can cause tracking errors with signals coming from WAAS satellites.

This work has shown that C/A code interference can induce tracking error of several meters in situations where:

- Doppler collision with Doppler difference lower than the DLL bandwidth,
- PRN code cross-correlations exhibit peaks,
- Navigation messages are correlated.

A great number of applications have low relative Dopplers (SBAS, pseudolites) and can thus be affected by this interference.

Fortunately, in this case, carrier smoothing gives good mitigation and unlike a multipath interference situation, the receiver can provide the interfering signal parameters (C/No, delay, phase and Doppler) and thus a correction algorithm can be developed [3].

In the future GEO satellites with ionic propulsion subsystem might have even lower Doppler variations leading to increased periods with code interferences.

This study could be extended in the future for SBAS L5/E5a quasi-stationary codes and possible future MBOC signals broadcasted by new versions of EGNOS, WAAS and other equivalent systems.

ACKNOWLEDGMENTS

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The authors also thank EGNOS PACF for providing RIMS data in the frame of the study.

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